

Jet Propulsion Laboratory  
California Institute of Technology

# Estimation of Benthic Reflectance with Bayesian Linear Mixture Models

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# Adapted from....

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Airborne mapping of benthic reflectance spectra with Bayesian linear mixtures



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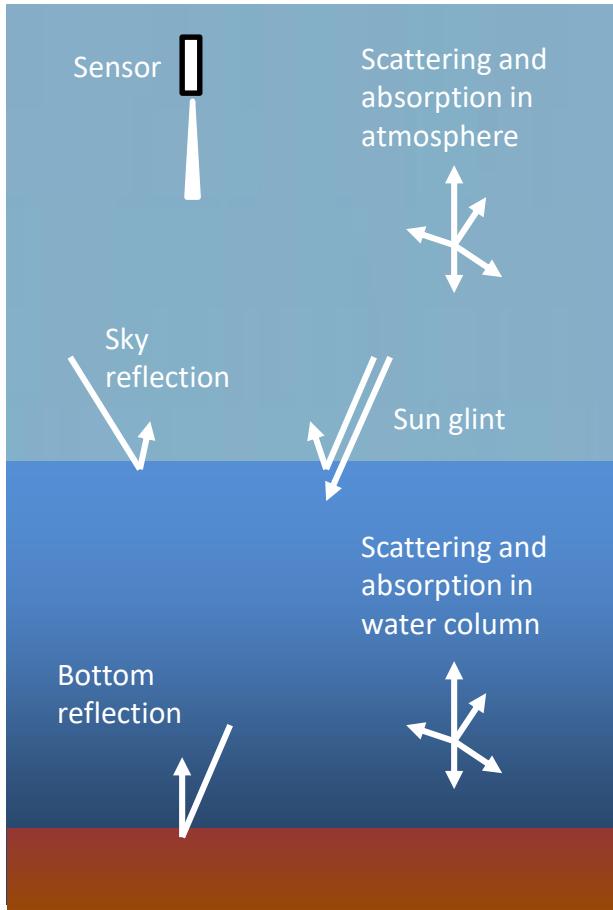


# Agenda

- Water column estimation algorithm
- Validation with CAO Hawaii data
- Initial maps from CORAL Hawaii data



# Major steps



## Retrieved quantities

### Step 1

Aerosol optical depth  $\tau$

Aerosol type  $\zeta$

Water leaving reflectance  $R_{rs}$

### Step 2

Glint-corrected  $R_{rs0}$

### Step 3

Backscatter  $b_b$

Attenuation  $K_d$

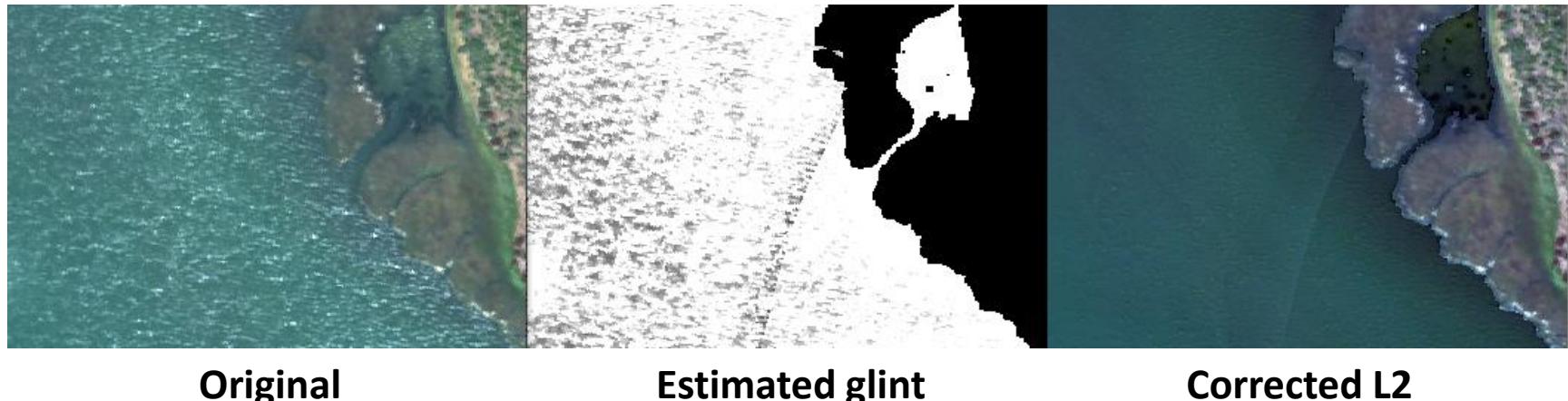
Depth  $H$

Benthic reflectance  $R_b$



# Glint correction

Glint is (approximately) spectrally uniform, so we can estimate it using “dark” NIR bands and subtract this contribution from the other channels [Gao et al., 2010].



Incorporating air/water interface correction, for water leaving reflectance below the surface:

$$R_{rs0} = \frac{R_{rs} - q}{1.562(R_{rs} - q) + 0.518}$$

Glint contribution



Adapted from [Lee et al., Applied Optics 37(27) 1998.]

# $R_b$ Inversion Procedure

Posit the relation [Maritorena et al., 1994]:

$$R_{rs0} = R_{inf} + (R_b - R_{inf}) e^{-2K_d H}$$

↑                      ↑                      ↑

bb / (2 $K_d$ )      Benthic reflectance      Attenuation

Depth



# $R_b$ Inversion Procedure

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bb / (2K<sub>d</sub>)      Benthic reflectance      Attenuation

Depth

**Problem: underdetermined**

$K_d$ , bb, and  $R_b$  yield  $(3N + 1)$  parameters for just N measurements



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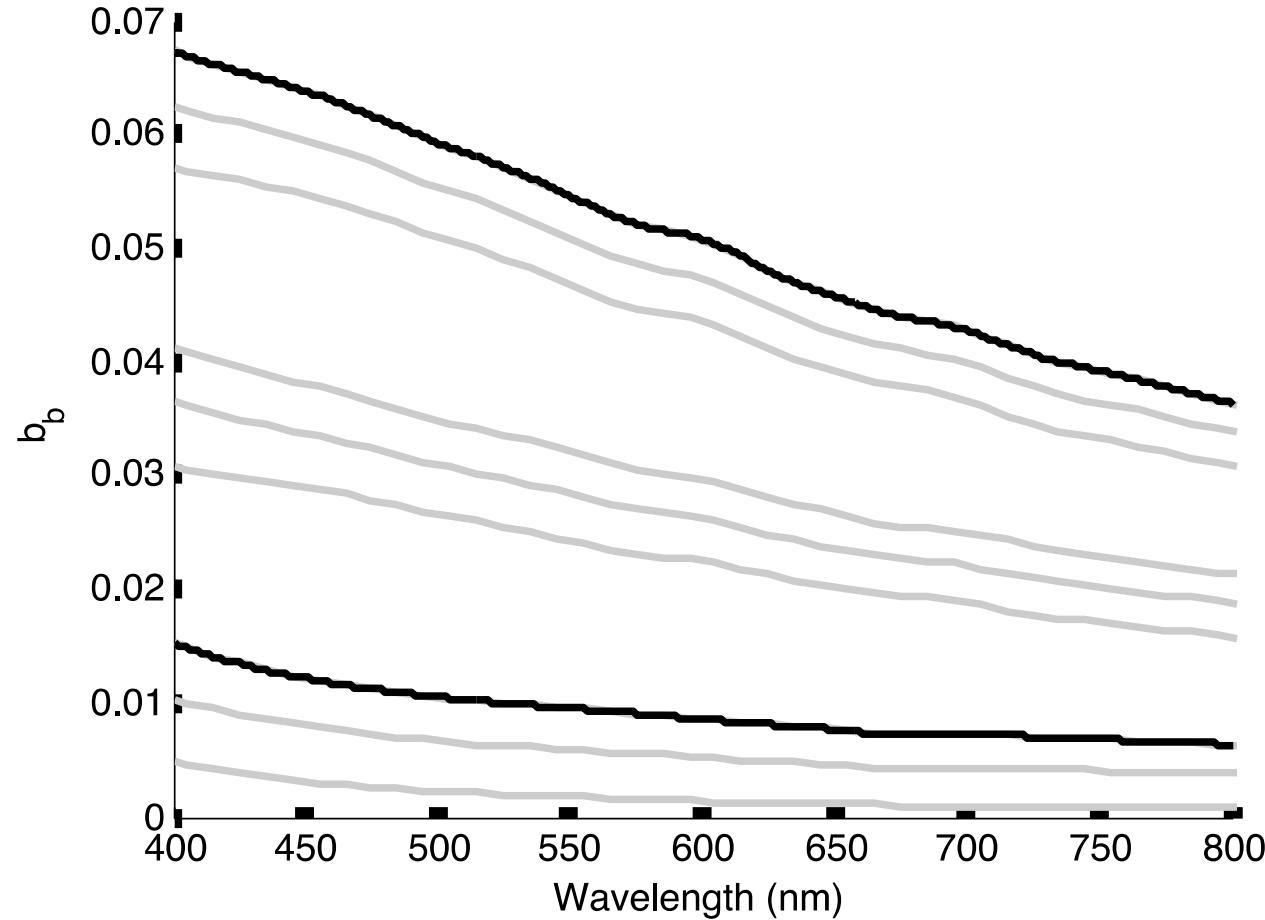
$K_d$ , bb, and  $R_b$  yield  $(3N + 1)$  parameters for just N measurements

**Solution: represent as linear mixtures**

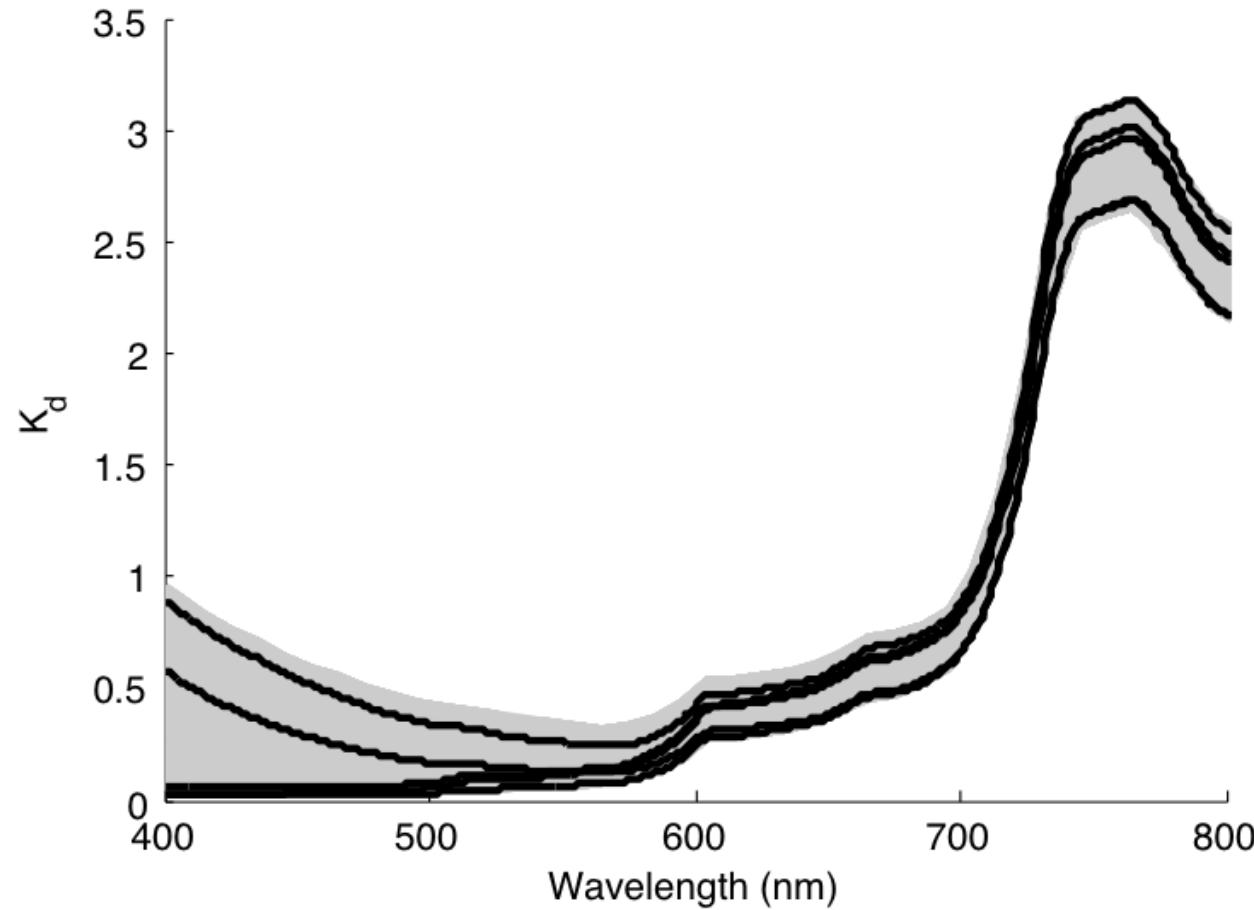
Parameterize  $K_d$ , bb, and  $R_b$  as nonnegative linear combinations of endmember spectra, and retrieve mixing coefficients (~20 DOF)



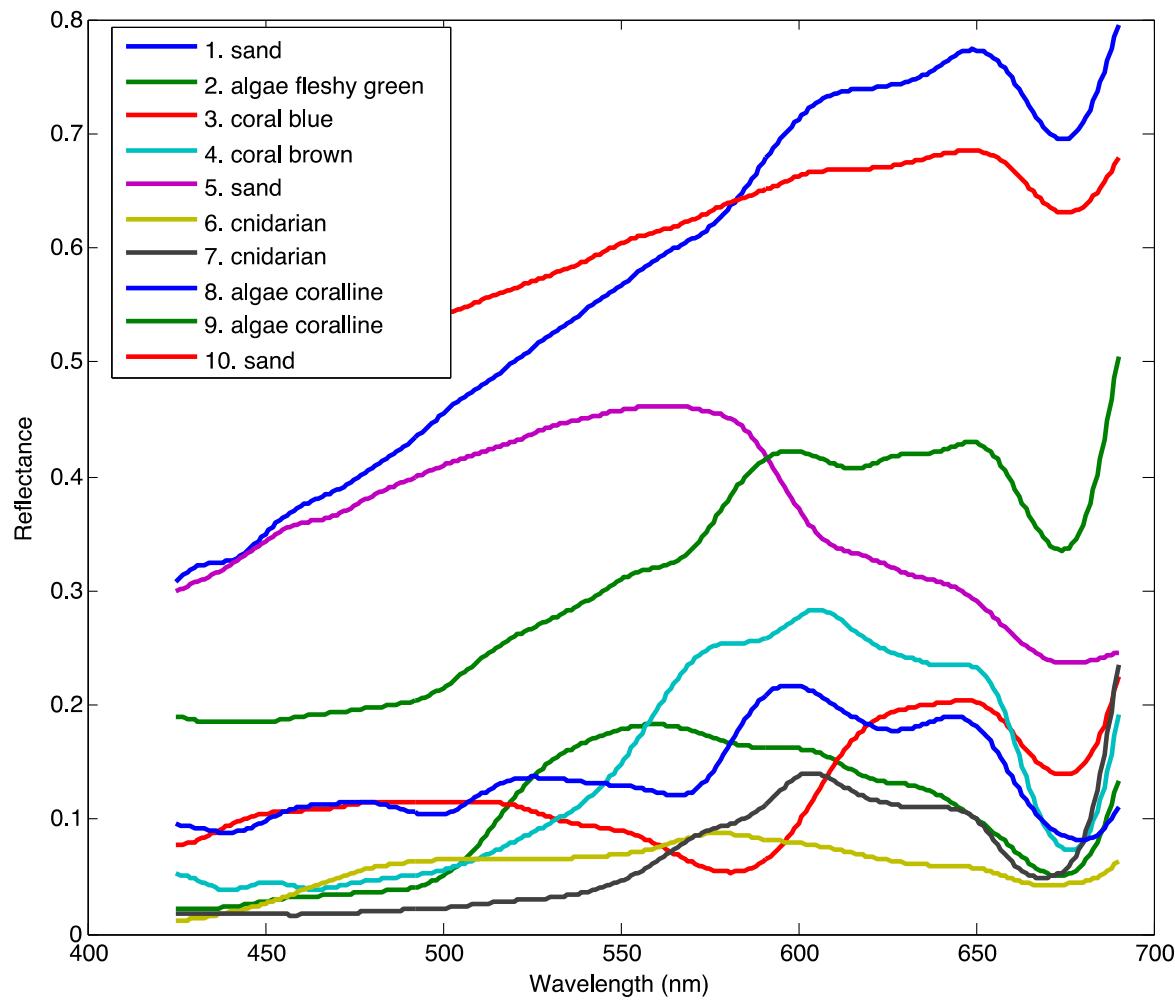
# Example of $b_b$ endmember library



# Example of $K_d$ endmember library



# Example of $R_b$ endmember library



# Procedure

Posit the relation [Maritorena et al., 1994]:

$$R_{rs0} = R_{inf} + (A - R_{inf}) e^{-2K_d H}$$

bb / ( $2K_d$ )      Albedo      Attenuation      Depth



# Procedure

Posit the relation [Maritorena et al., 1994]:

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bb / ( $2K_d$ )                          Albedo                          Attenuation                  Depth

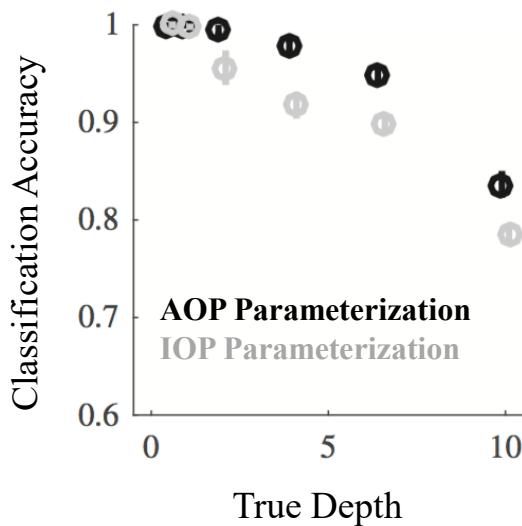
Optimize via Levenberg Maquardt, minimizing:

$$\begin{aligned} \text{Error}(x) = & (R_{rs0} - R_{rs0}^*) \quad \leftarrow \text{Model fit vs. measurement} \\ & + \alpha_{bb590} (\mu_{bb50} - bb_{590}^*) \\ & + \alpha_{kd450} (\mu_{kd450} - K_{d450}^*) \\ & + \alpha_{kd590} (\mu_{kd590} - K_{d590}^*) \\ & + \alpha_H (\mu_H - H^*) \end{aligned} \quad \left. \right\} \text{Statistical priors to constrain the other free parameters}$$



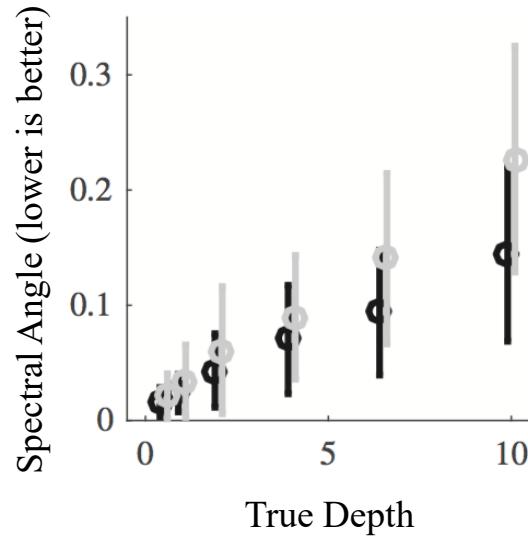
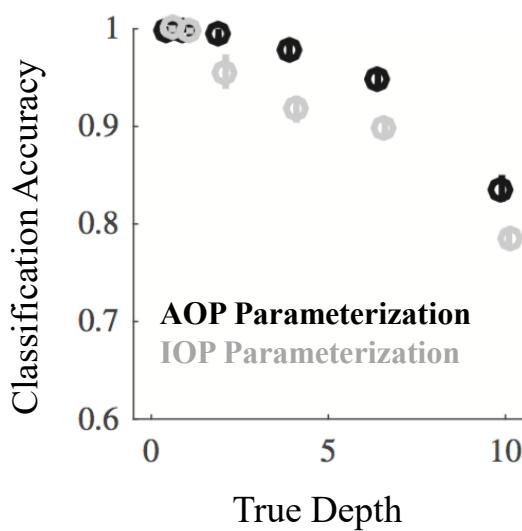
# Retrieval performance simulation

- Apparent Optical Property and Intrinsic Optical Property parameterizations
- In AOP Depth and  $R_b$  are decoupled through an extra degree of freedom
- IOP gives best absolute depth, AOP gives slightly better  $R_b$  fidelity



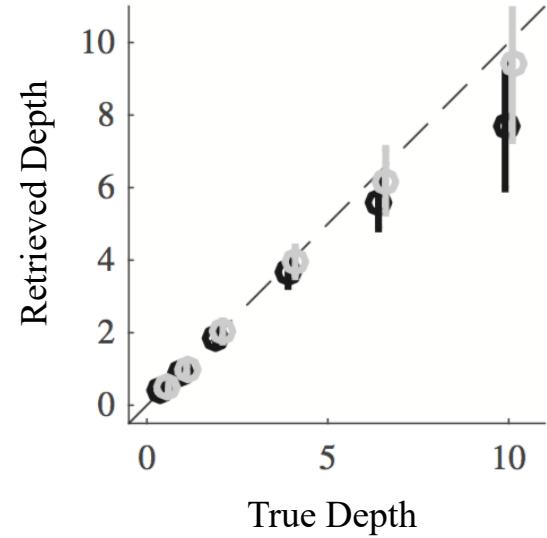
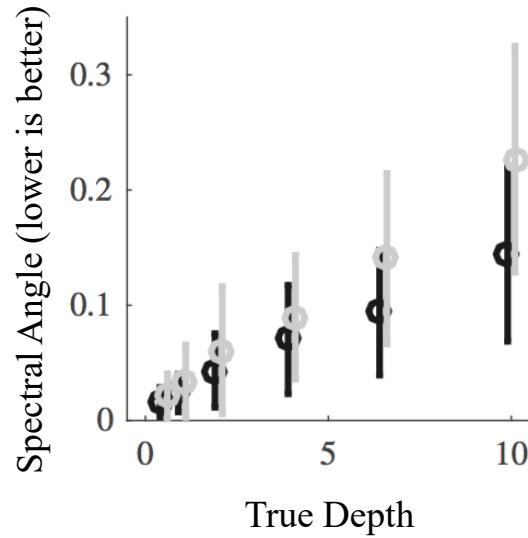
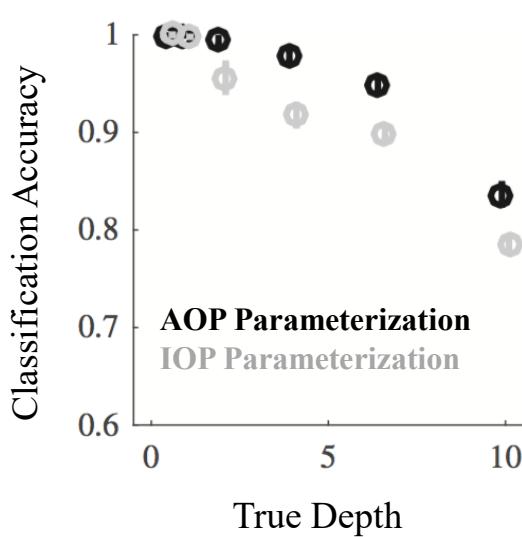
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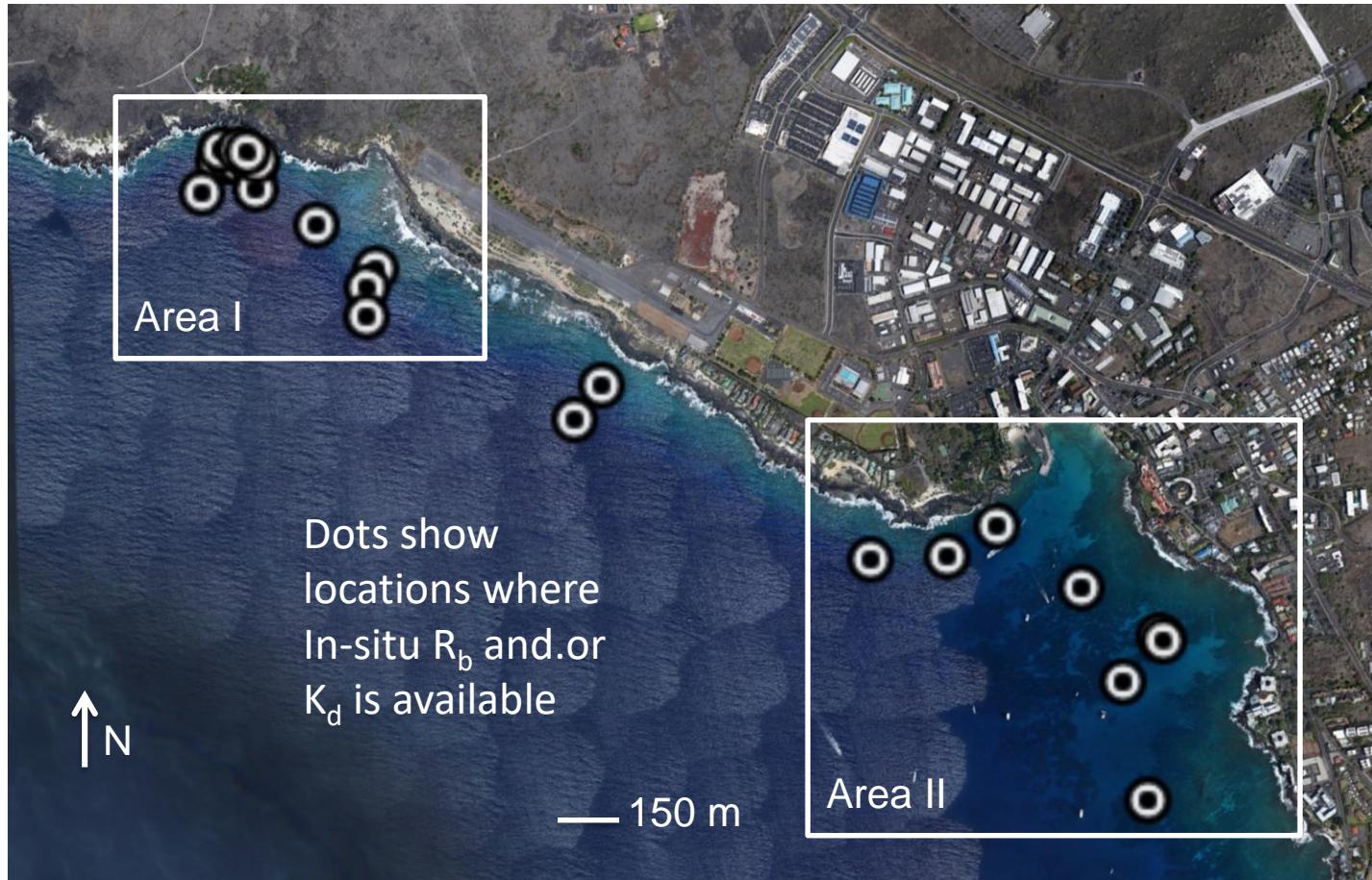


# Agenda

1. Water column estimation algorithm
2. Validation with CAO Hawaii data
3. Initial maps from CORAL Hawaii data



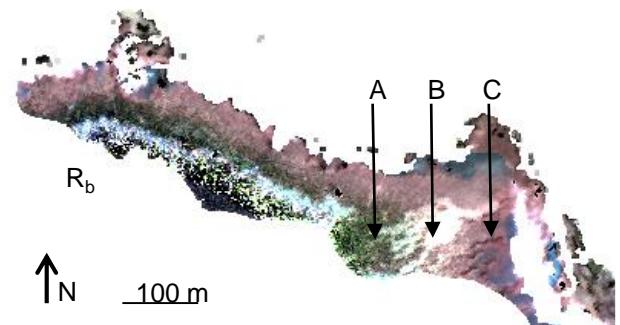
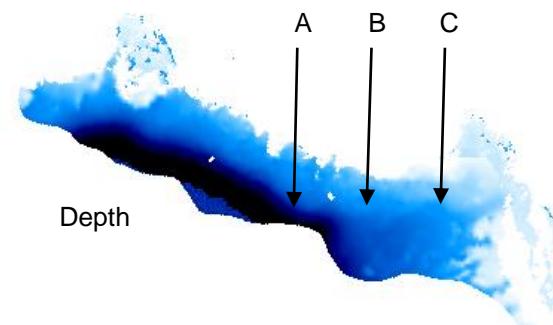
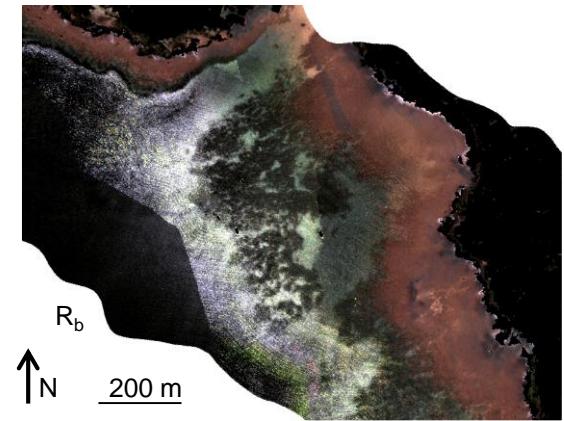
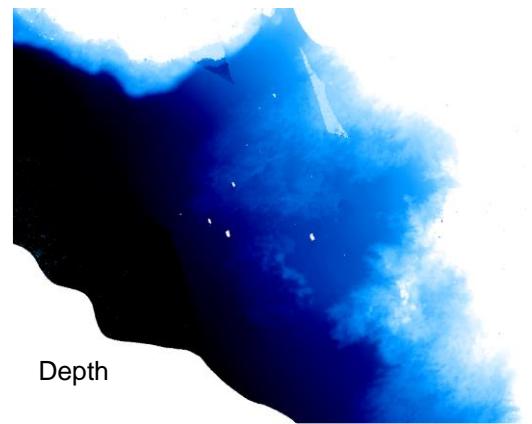
# Validation sites



Airborne VSWIR data collected by the Carnegie Airborne Observatory



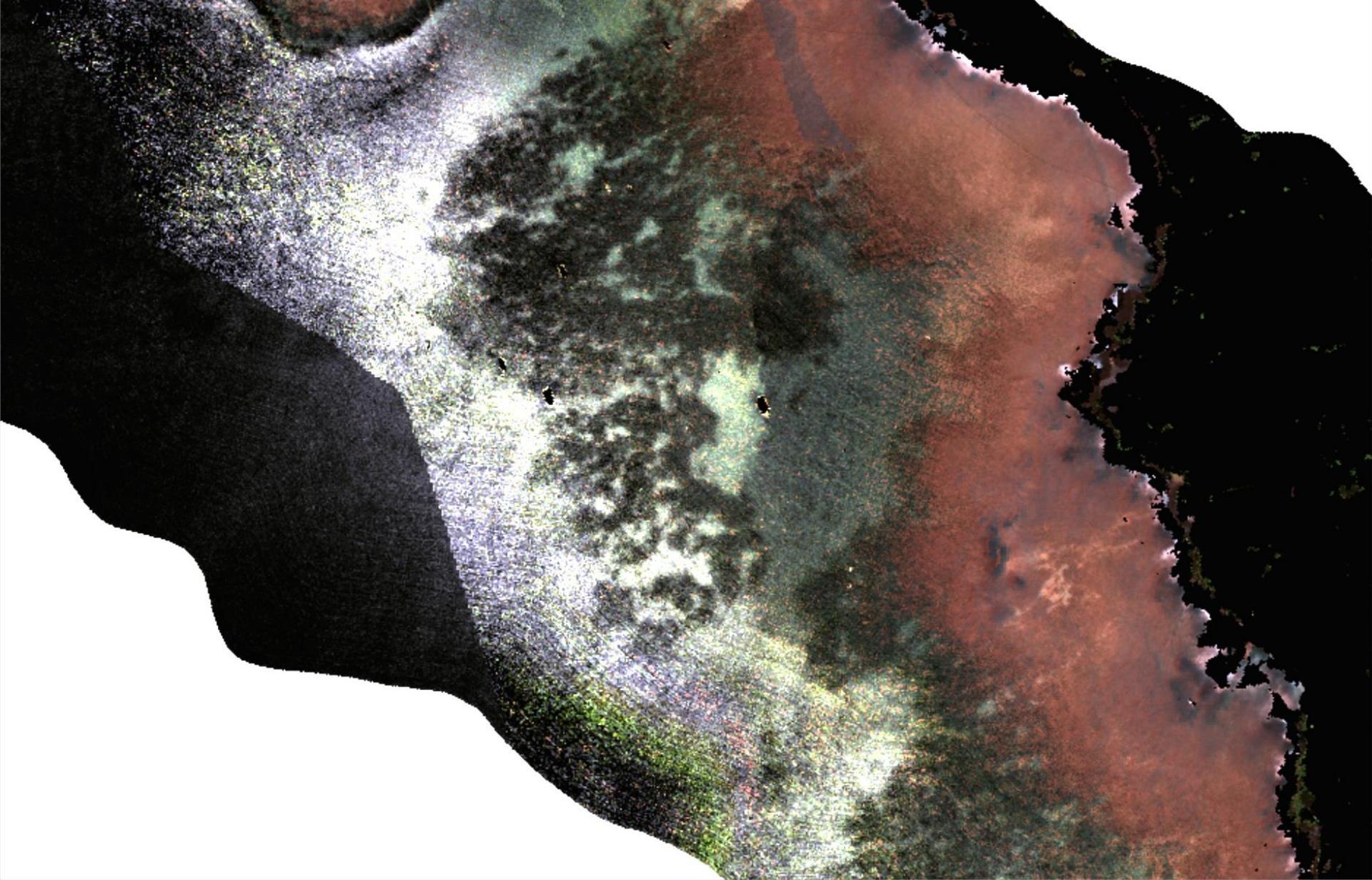
# Benthic reflectance maps



Airborne VSWIR data collected by the Carnegie Airborne Observatory

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Airborne VSWIR data collected by the Carnegie Airborne Observatory

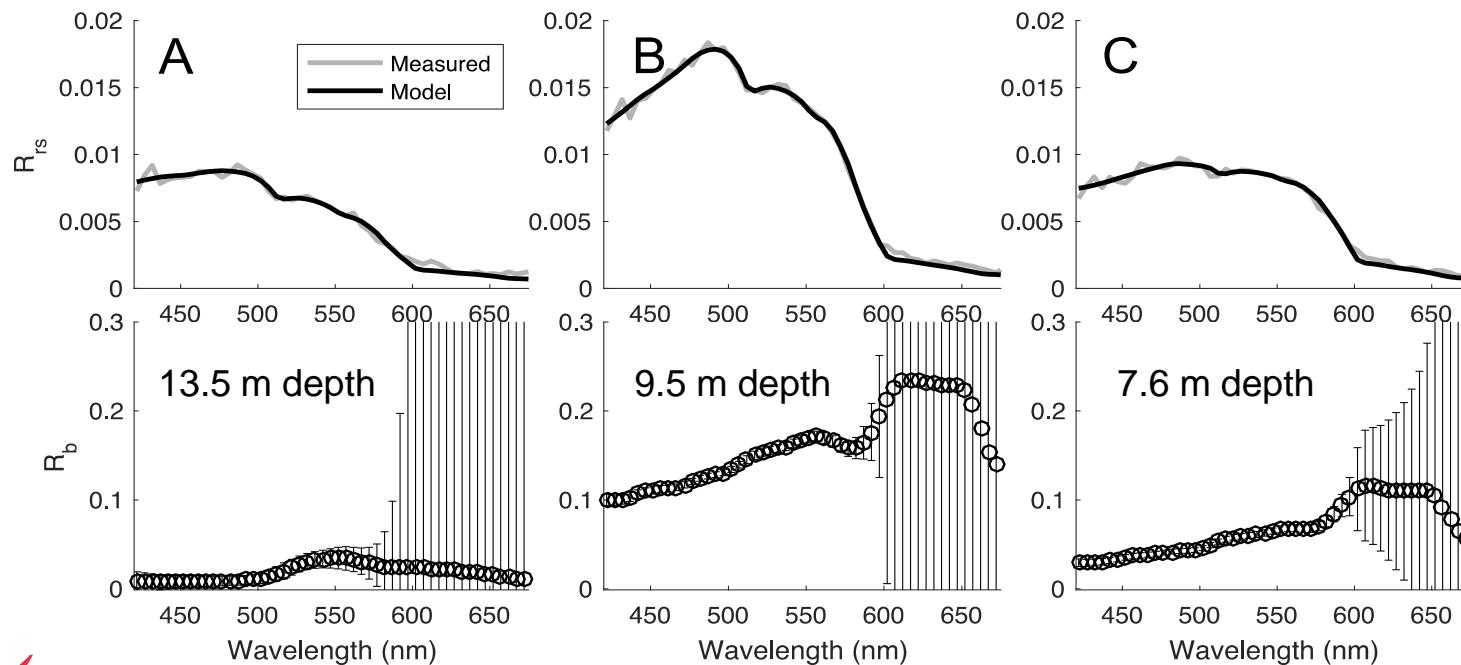
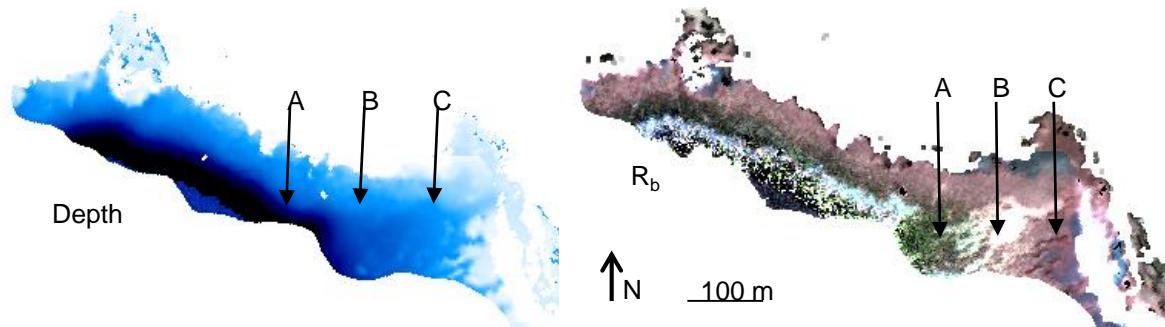
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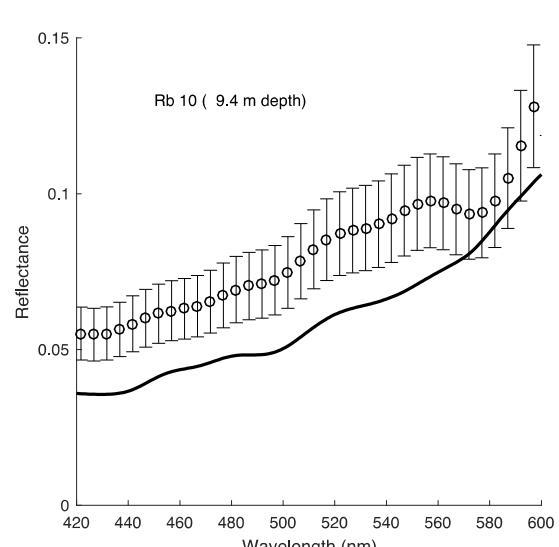
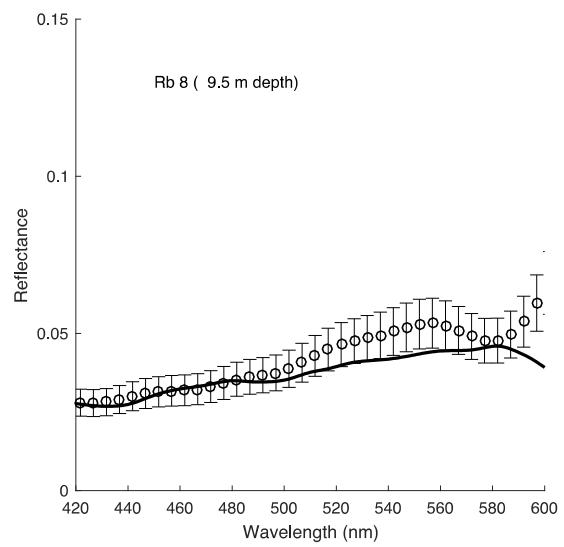
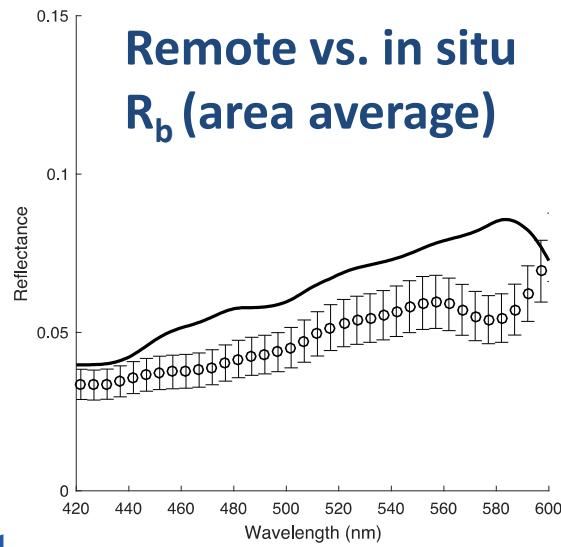
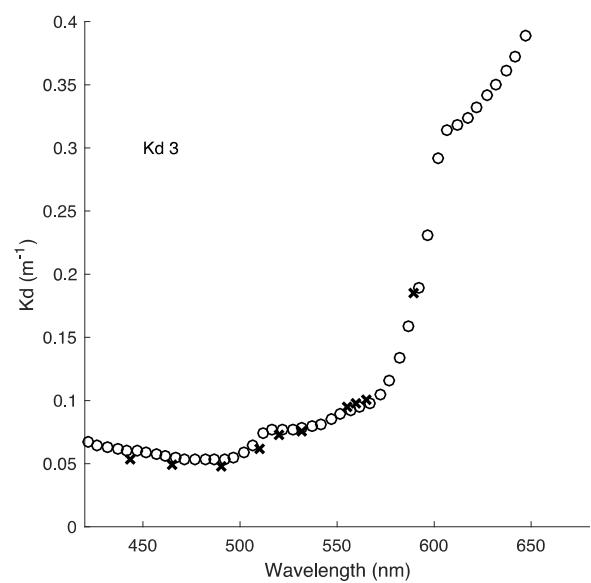
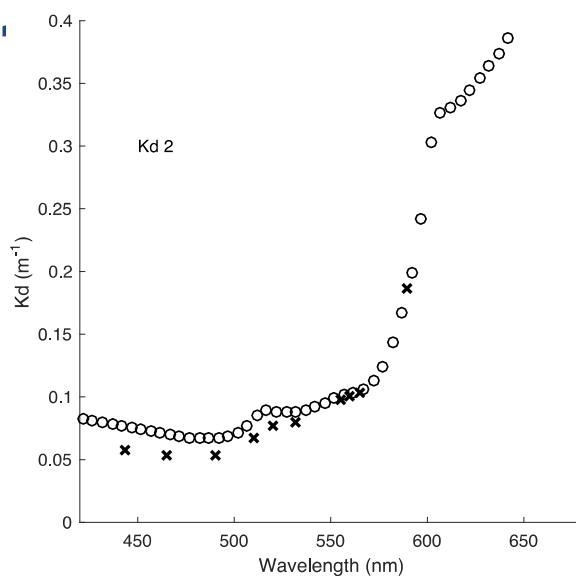
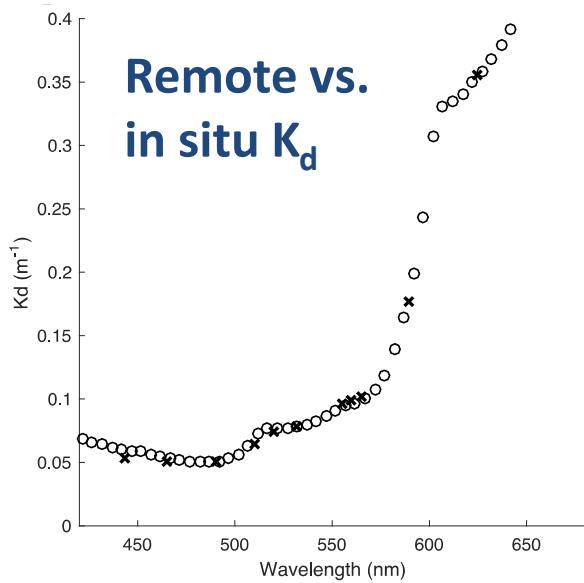
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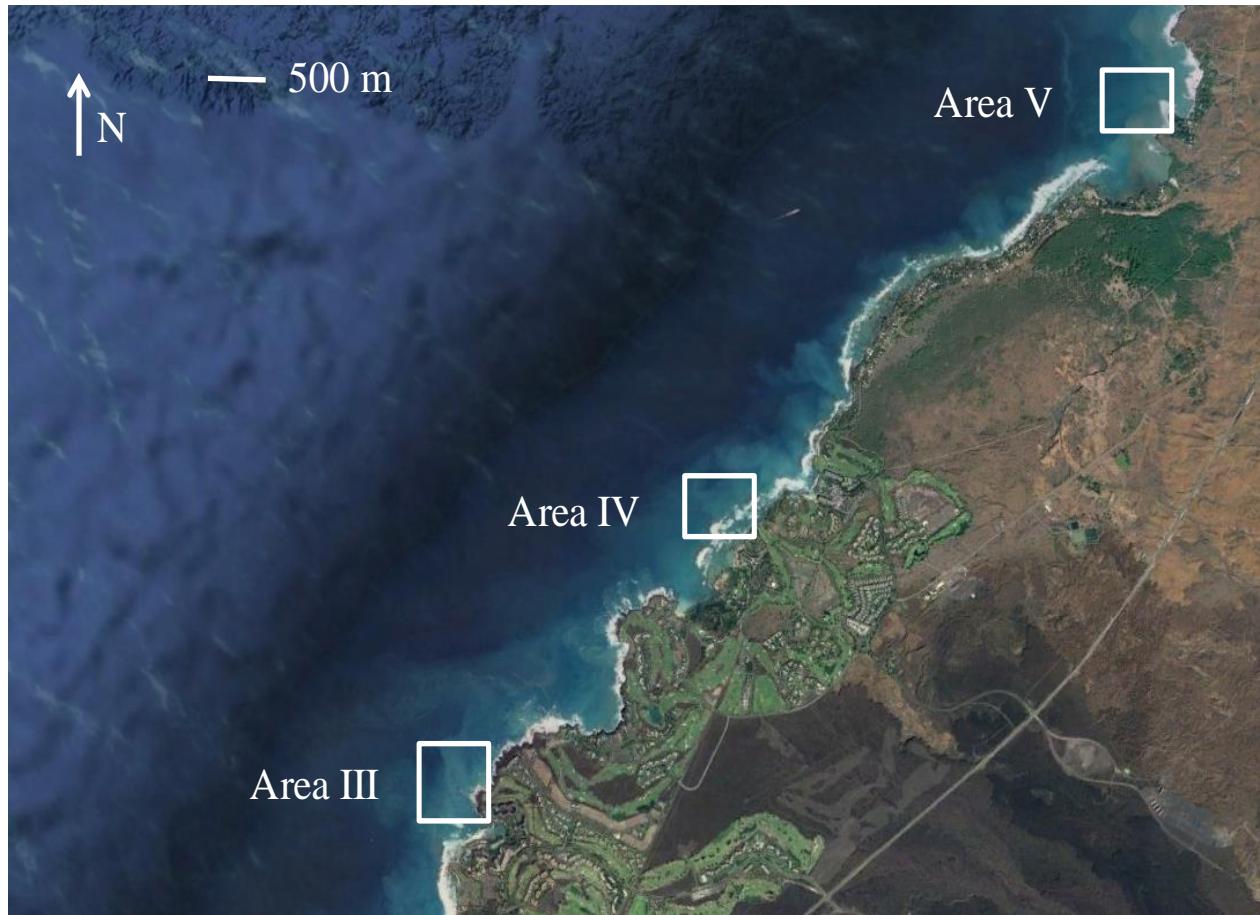
# $R_{rs}$ and Bottom Reflectance

Airborne VSWIR data  
collected by the  
Carnegie Airborne  
Observatory (CAO)





# Depth Validation sites



Airborne VSWIR data collected by the Carnegie Airborne Observatory



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# Depth vs. SHOALS (2001) Lidar

Site III



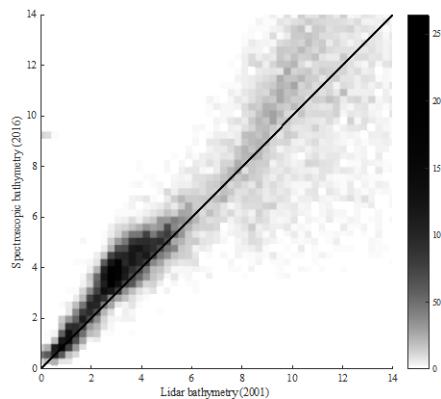
Site IV



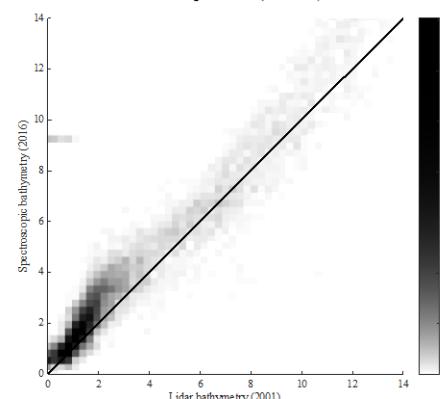
Site V



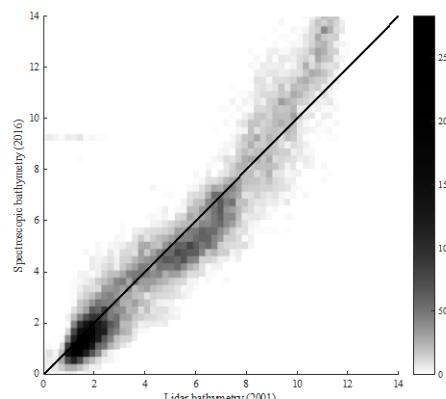
Comparison (Counts)



Comparison (Counts)



Comparison (Counts)



Airborne VSWIR data collected by the Carnegie Airborne Observatory

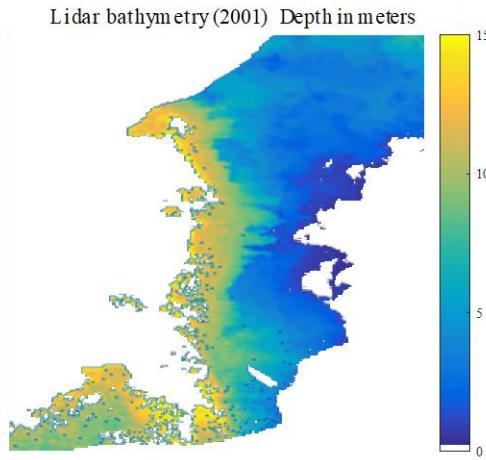
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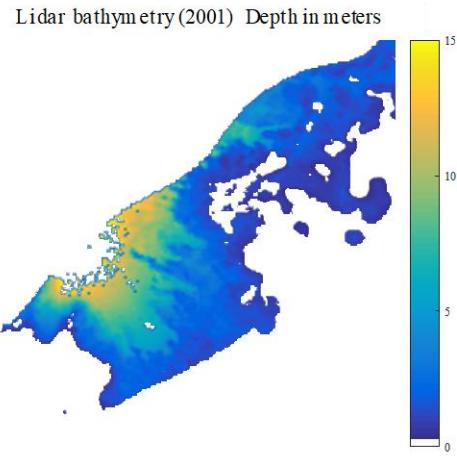
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# Depth vs. SHOALS (2001) Lidar

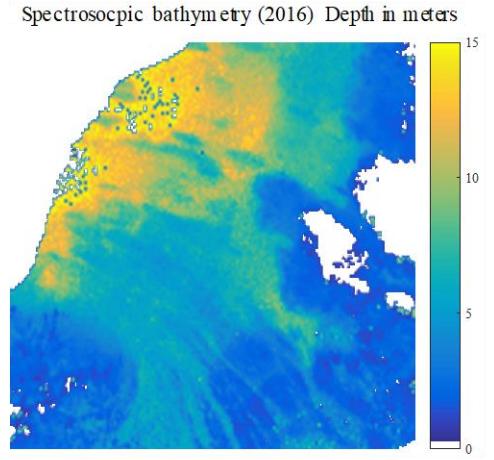
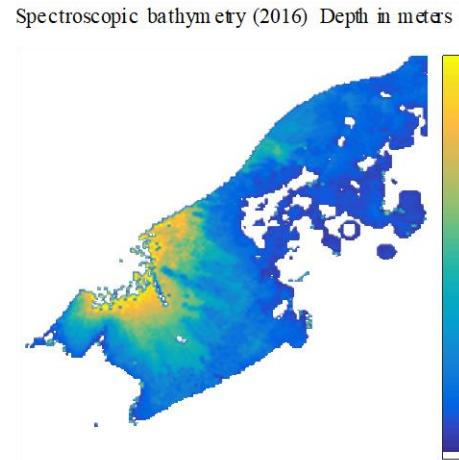
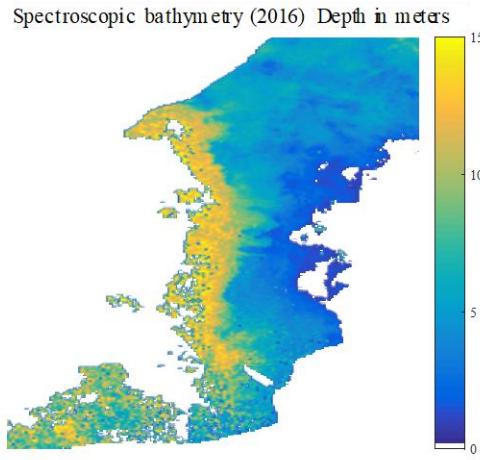
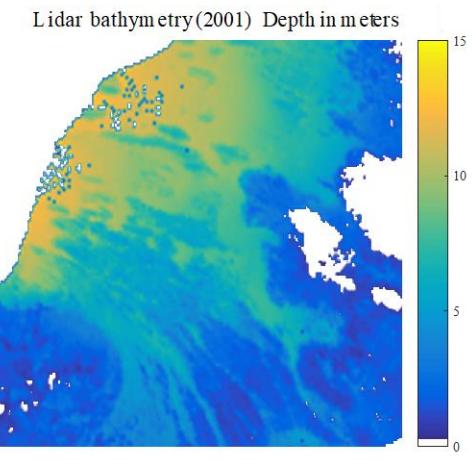
Site III



Site IV



Site V



Airborne VSWIR data collected by the Carnegie Airborne Observatory

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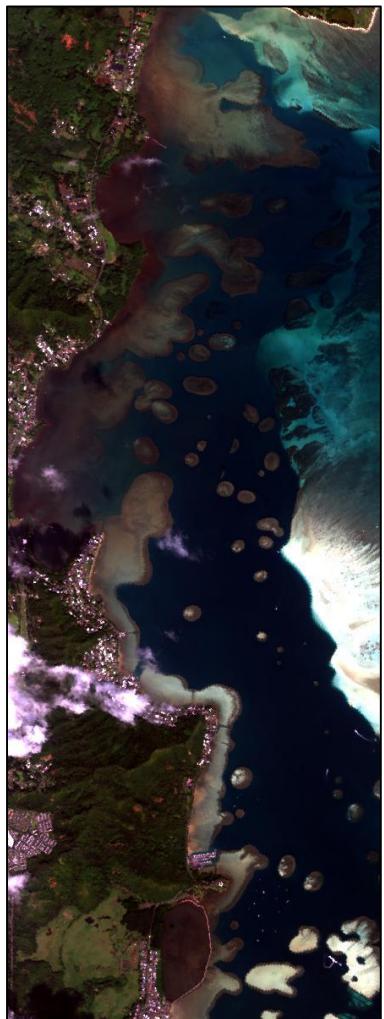
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# Agenda

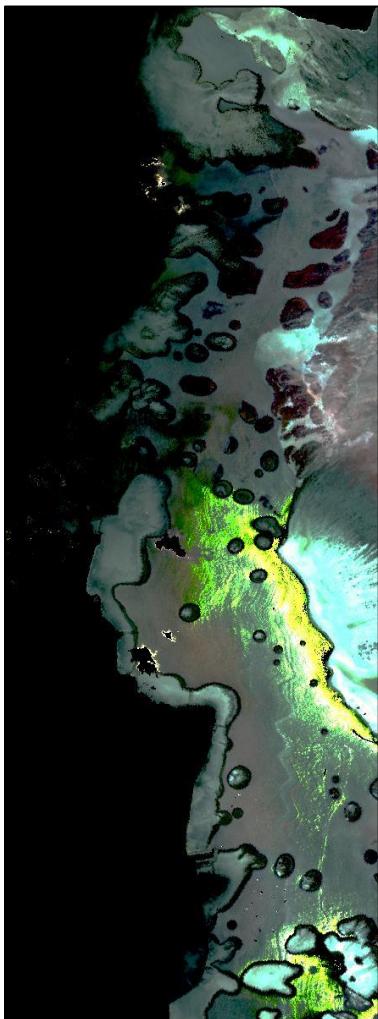
1. Water column estimation algorithm
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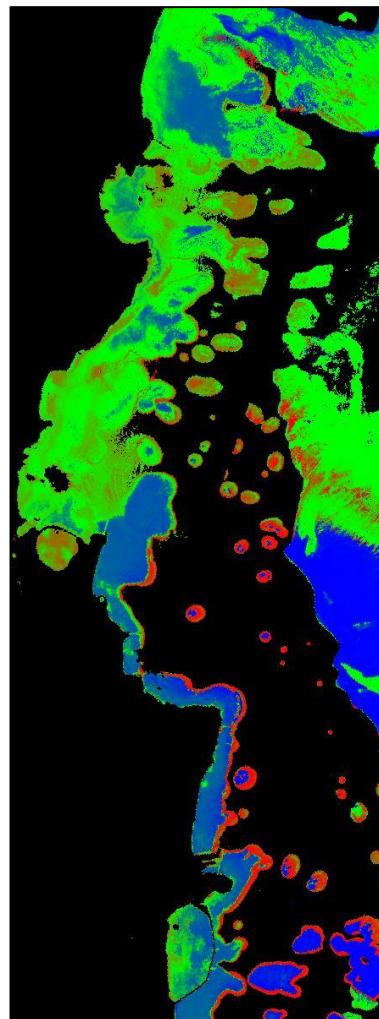
**Water-leaving  
Reflectance**



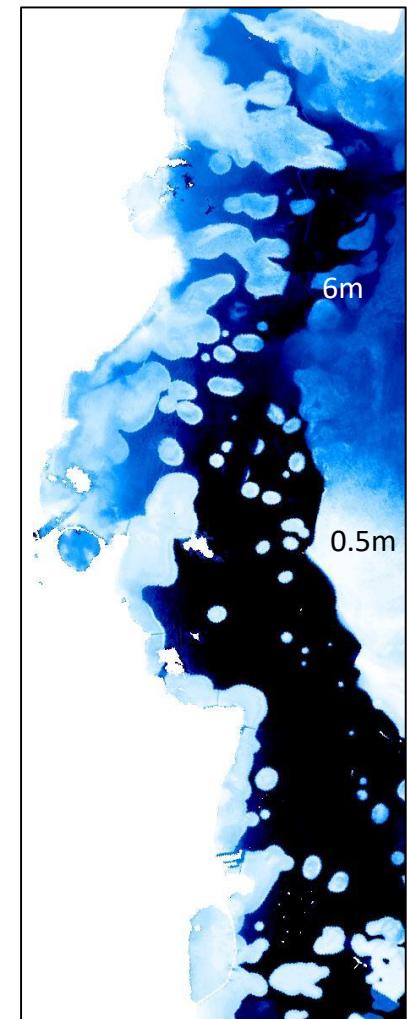
**Benthic  
reflectance**



**Coral Algae Sand**



**Depth**

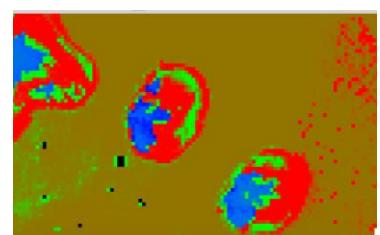
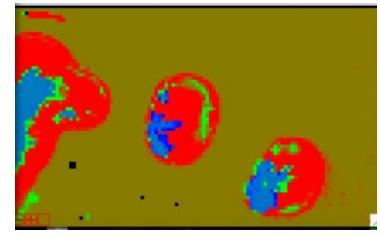
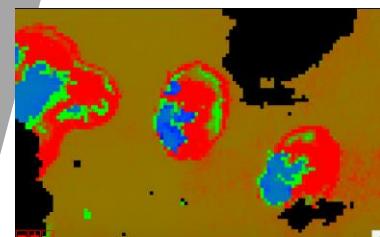
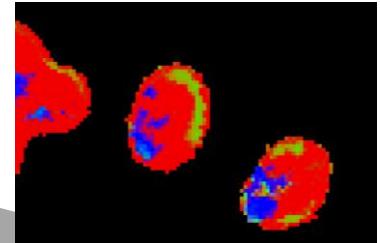
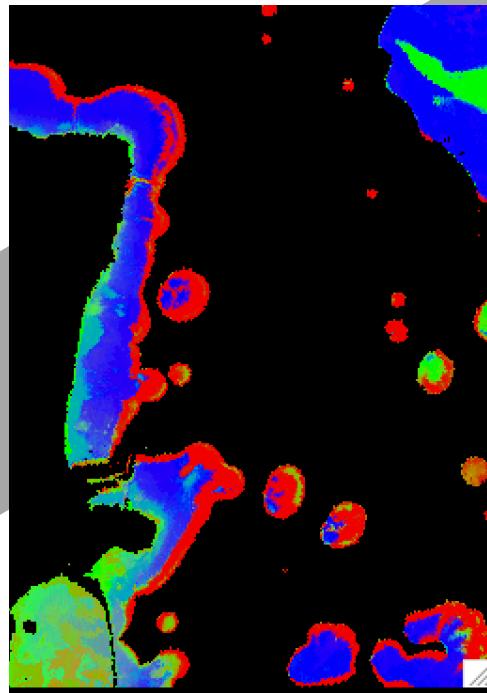


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# Consistency check

Overflights in 2016  
and 2017



# Thanks!

- **NASA Earth Science Division** and the Earth Venture Suborbital program
- **The Carnegie Institute for Science**, for use of Carnegie Airborne Observatory data in this pilot project
- **The PRISM and CORAL teams**

